



# High Frequency Modeling of Transformer Using Black Box Frequency Response Analysis

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**Abstract**—Lightning Surges consequently induce high frequency overvoltage to transformers. Therefore, it is alluring to study the transfer voltage of lightning surges from primary to secondary side of transformer. Keeping in mind the end goal to do lead this review, high frequency Siemens power transformer of rating 25KVA, 25KV/400V is to be examined. In this paper, an advanced and modified high frequency model of transformer is presented for protection of load against lightning transients. Suggested model is modified form of N.A Sabiha model and based on black box, two ports four terminal network theory. For No load condition, Transformer parameters are calculated on two resonance frequencies of 450 KHz & 1 MHz using fast Fourier transform. Matlab/Simulink is used for simulation analysis. Both Time and frequency domain validate the accuracy. Resemblance between the measured and calculated results confirms the precision of proposed model when an impulse of 1.2/50 $\mu$ s is applied to transformer terminals.

**Index term**—Power transformer, Black box analysis, Frequency response analysis, resonance frequency.

## I. INTRODUCTION

Lightning surges shifted to consumer low voltage side through the interwinding capacitance of transformer. So, it is paramount importance to design the transformer to withstand the high voltages and high frequency stresses during lightning. Lightning impulse test devised to proof the high frequency behavior of transformer [1]- [3]. Different high frequency protected models from lightning are Proposed to study the transient behavior of transformers for both loaded [4]- [6] and unloaded conditions [7]- [10]. The high-frequency behavior can be model by different ways.

In mechanical way computing a lumped electrical system in the light of geometry, winding stresses during transients and material properties, yet requires mechanical detailed data like winding material, gap between windings, physical structure, material properties including dimension and core size, about

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the transformer [11]- [12]. Winding deformation can be calculated by FRA using finite element method. Conditional monitoring of large power transformer using SFRA is presented in [13]. Using frequency analyzer, the values for L, R and C were calculated for equivalent model of transformer. When inductance increases then disk deformation and local breakdown occur. Value of resistance is dependent on resonance frequency. The desirable mechanical data is hardly ever provided by the transformer manufacturer.

When detailed data and internal structure of transformer is not present, black box model is appropriate to acquire high frequency behavior of transformer [4]- [5], [9]- [10], [14]- [16]. In [17] M Heindl compares white box, gray box and black box model. In White box model complexity is high; bandwidth is low as compared to gray and black box. But it allows deeper system view. While gray box lies between white and black box model. In [18] artificial method is used for gray box analysis of transformer parameter calculations. The numbers of unknown parameter are reduced using both Weibull Distribution function and exponential function. In [19] capabilities of a black box model were analyzing to characterize the transformer at high frequency. Measured values and simulated values in EMTP-RV for transmitted over-voltages are compared.

Black Box model has several terminals and based on terminal measurements. While in [4] N.A Sabiha presented transformer model for dual resonance frequencies which is based on two ports four terminals network theory. Aforesaid model is modified form of [9] Piantini model, based on single resonance frequency. In aforesaid model resonance frequency is calculated by transfer function. The high frequency behavior of power transformer based on several resonance points in a wide frequency band is due to inductive and capacitive behavior of transformer [15]. Frequency band is divided into low, medium and high frequencies but these levels do not have distinct boundaries. The transformer equivalent T or Pi model is based on lumped parameters.

In [20] transfer of surges from primary to secondary side and effect of internal capacitance on winding skin effect of transformer were determines. In proposed model, the parameters were determined by frequency-characteristic measurement using an impedance analyzer. Hysteresis and saturation effect not discussed because CIGRE WG suggested that the hysteresis effect can be neglected in lightning surges. Similarly, Penetration of magnetic flux can be neglected at 1MHz frequency or for higher frequencies. In his model, various surges calculation is carried out by EMTP.

In [7] PTM Vaessen proposed transformer model for high frequencies. The Proposed model was for no load condition and based on black box analysis. For value of inductance (L) the value for frequency  $\omega$  will be minimum or nearly equal to zero and for the value of capacitance (C) the value of frequency  $\omega$  is very high nearly equal to infinity. The value of L and C determined from imaginary part of  $Z(i\omega)$ .

In [21] transformer winding parameters like R, L and C matrices were found using numerical method for lightning test. In [22] the transformer modeling is optimized using genetic algorithm and one of important application in fault detection is discussed. Some recent models of transformers have been developed in [23]- [26] to study the transferred surges and fault diagnostic techniques by using a program of transition electromagnetic called EMTP/ATP and Orcad-Pspice.

However, all these models need some sophistication. So, modified model of power transformer at two resonance frequencies is presented here.

## II. TWO PORTS NETWORK THEORY

Two ports network theory is used to determine the Z-Parameters (impedances), Y-parameter (Admittance), H-parameters (Hybrid) and T-Parameters (Transmission). In this theory two ports have four terminals and Network is represented by black box. The driven source may be voltage or current. But here the driven source is impulse voltage. Based on connection of impedances, two ports network can be classified into T or  $\pi$  (Pi) network. Using open circuit test, we determine the different parameters of T-model transformer. The linear T-network equations are

$$V_p = I_p * Z_{11} + I_s * Z_{12} \quad (1)$$

$$V_s = I_p * Z_{21} + I_s * Z_{22} \quad (2)$$

When impulse is applied on primary side of transformer and secondary remain open then we find the following quantities.

$$Z_{11} = \frac{V_p}{I_p} \mid I_s = 0,$$

$$Z_{21} = \frac{V_s}{I_p} \mid I_s = 0$$

Similarly, when impulse is applied on secondary and primary remain open then we obtain

$$Z_{12} = \frac{V_p}{I_s} \mid I_p = 0,$$

$$Z_{22} = \frac{V_s}{I_s} \mid I_p = 0$$

## III. EXPERIMENTAL SETUP

The experiment was executed in High Voltage Lab ESEIAAT\_TRI of Universitat Politècnica de Catalunya (UPC)-Technological University of Catalonia, Barcelona Spain. The rating of test transformer was 25KVA, 25KV/400V DYN5 (Delta start connected with earth neutral).



Fig1. Experimental setup for transformer testing

Impulse of 4KV applied to primary side of transformer while secondary side remained open and find out the primary current ( $I_p$ ), primary voltage ( $V_p$ ) and secondary voltage ( $V_s$ ) as shown in Fig2. Fours channel oscilloscope was used for captures the wave foams and save their data in time domain.

After taking the values of  $V_p$ ,  $I_p$ , and  $V_s$ , convert these wave foams into discrete values. Then find out the transfer function

$$T(s) = V_{out}/V_{in}$$

From this T(S), find the two resonance frequencies. The resonance frequencies are at 450 KHz and 1 MHz. For these resonance  $Z_{11}$  shows capacitive behavior.

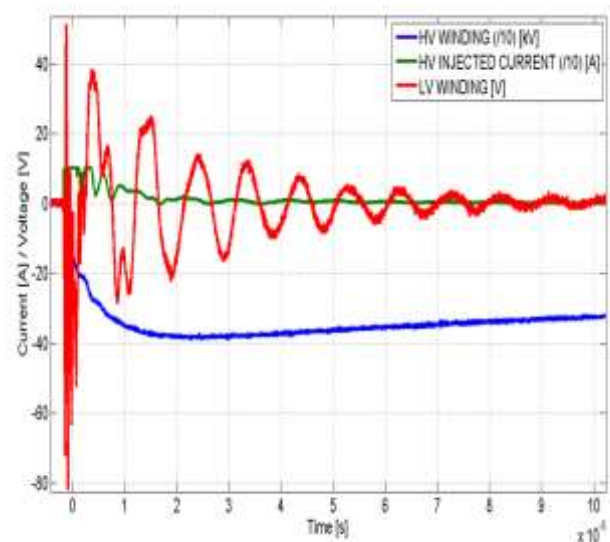


Fig2. Impulse Voltage on HV side, Impulse current On HV Side, and Secondary voltage.

Similarly, when impulse applied on secondary side of transformer and primary side was kept open circuit then calculate the value of  $V_s$ ,  $I_s$ , and  $V_p$  as shown in figure 3.

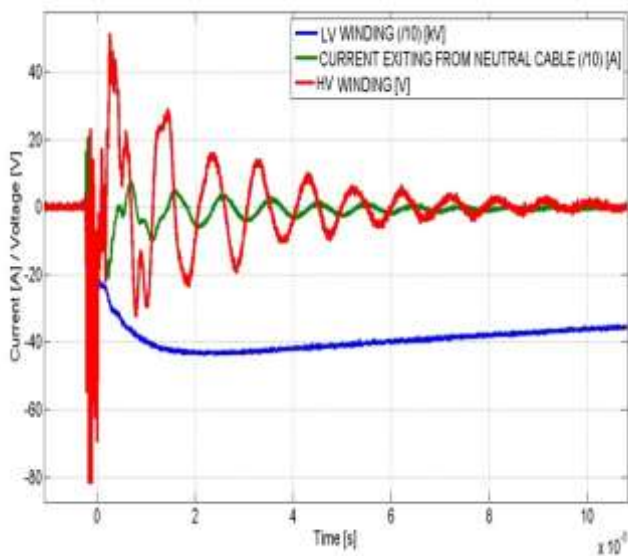


Fig3. Impulse Voltage on LV side, Impulse current on LV side, and Primary voltage

When impulse applied on secondary, transfer function for secondary side was calculated. T(S) verifies that Z12 and Z21 both resonate on same frequency as shown in fig 4. From this T(S), find the two resonance frequencies for which Z21 have inductive behavior.

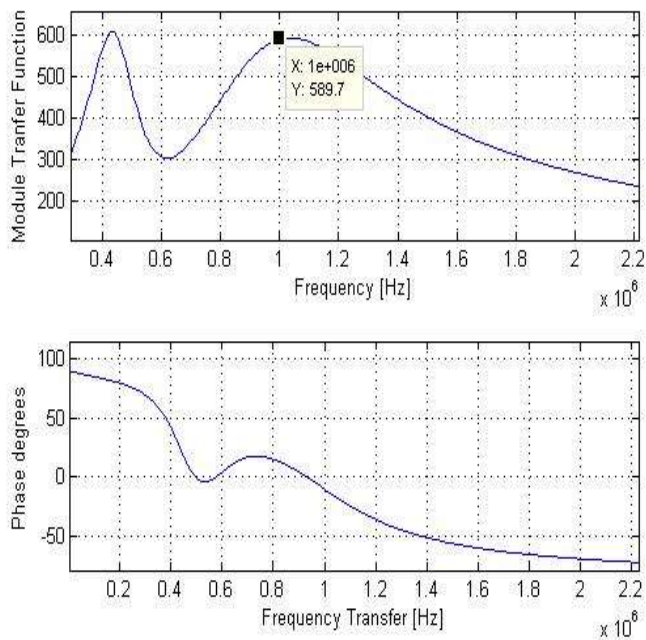


Fig 4: Transfer Function for Z12 and Z21

Apply the Fast Fourier transform to the discrete data of these currents and voltages wave foams and using transfer function method find out the values of parameters. Amplitude of Z11 and phase angle is given in figure 5.

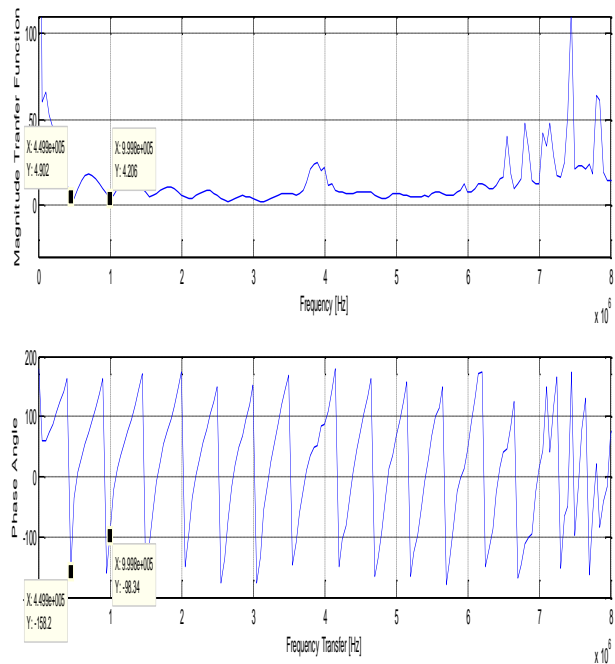


Fig 5: Magnitude and Phase angle for Z11

Negative value of the imaginary part of Z11-Z12 shows capacitive behavior of the transformer.

Similarly, the value of Z12 is shown in figure 6.

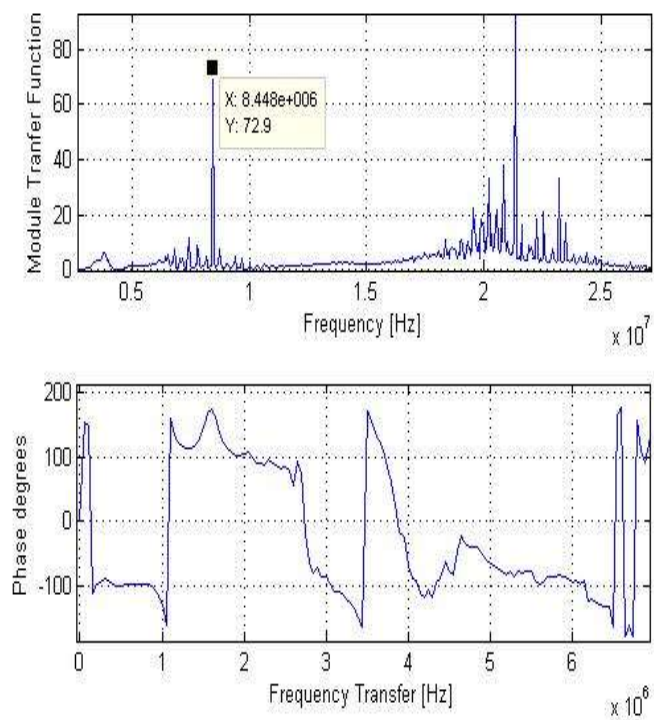


Fig6: Magnitude and Phase angle of Z12

The value of Z22 is shown in figure 7.

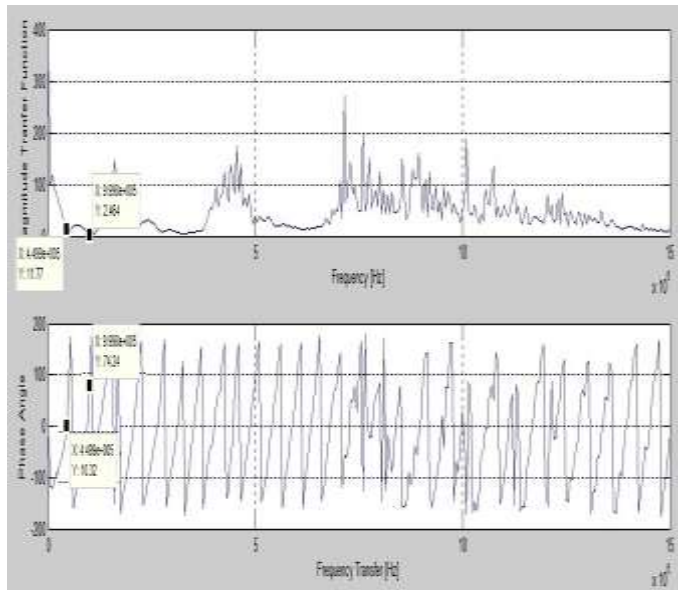


Fig7: Magnitude and Phase angle for Z22

Positive value of Z22-Z21 shows the inductive behavior of secondary side of transformer.

The value of Z21 is shown in figure 8.

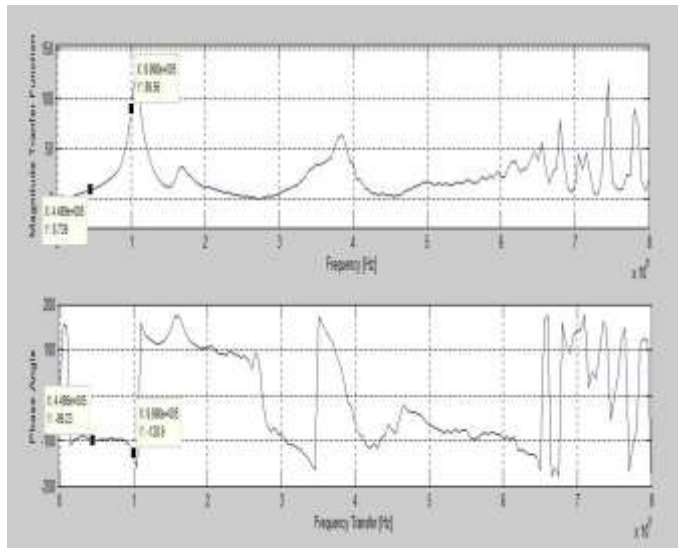


Fig8: Magnitude and Phase angle for Z21

From the impedances equations at resonance frequency calculate the values of R, L and C using the resonance equations.

TABLE I. THE VALUES OF PARAMETER OF PROPOSED TRANSFORMER

Elements	Values
R1	3.013 Ω
C1	0.20657315e-7
R2	0.624 Ω
L2	3.70244e-9H
R3	558.5405 Ω
L3	0.058967e-3H
C3	0.00043e-6F
R4	500 Ω
L4	0.067305e-3H
C4	0.001859e-6F
R5	12.54 Ω
L5	0.3748e-5H
R6	53.213 Ω
L6	1.123656e-5H

#### IV. PROPOSED MODEL

The proposed T- Model of the power transformer is shown in figure 9.

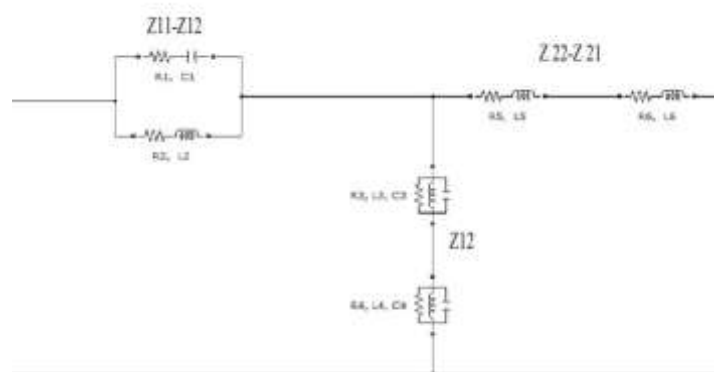


Fig9. Proposed T-Model for Transformer

The secondary transfer voltage of the propped model for unloaded condition with impulse is

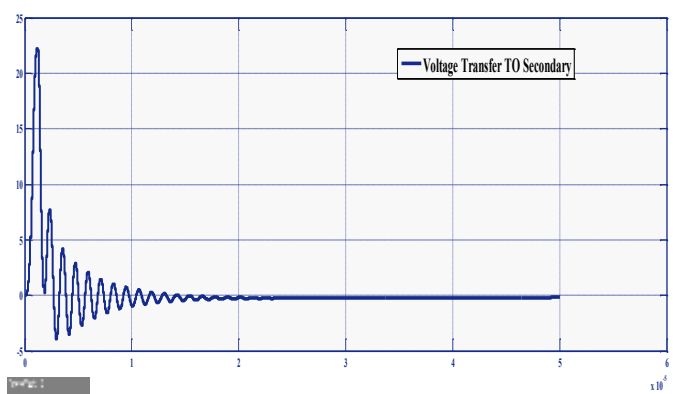


Fig10. Transfer voltage from primary to secondary side

### CONCLUSION

The modified model for transformer load protection from lightning surges of specific frequency is tested at 4KHz and 1 MHz. The resonance frequency for both Z12 and Z21 is same which validate the proposed model. Therefore, it can be very easily realized that the transformer model for protection of load from transients or lightning signal is very efficient. The proposed technique can be used for online conditional monitoring of transformer in future.

### REFERENCE

- [1] G. Liang, H. Sun, X. Zhang, X. Cui, "Modeling of transformer windings under very fast transient overvoltages" IEEE Trans. Electromagn. Compat., vol. 48, no 4, Nov. 2006.
- [2] M. Popov, L. van der Sluis, R. P. P. Smeets and J. L. Roldan, "Analysis of very fast transients in layer-type transformer windings", IEEE Trans. Power Del., vol. 22, no. 1, pp. 238-247, Jan. 2007.
- [3] K. Samarawickrama, N. D. Jacob, A. M. Gole and B. Kordi, "Impulse Generator Optimum Setup for Transient Testing of Transformers Using Frequency-Response Analysis and Genetic Algorithm," in IEEE Transactions on Power Delivery, vol. 30, no. 4, pp. 1949-1957, Aug. 2015.
- [4] Sabiha, Nehmdoh A., and Matti Lehtonen. "Lightning-Induced Overvoltages Transmitted Over Distribution Transformer With MV Spark-Gap Operation—Part I: High-Frequency Transformer Model." IEEE Transactions on Power Delivery 25.4 (2010): 2472-2480.
- [5] Sabiha, Nehmdoh A., and Matti Lehtonen. "Experimental verification of distribution transformer model under lightning strokes." Power Systems Conference and Exposition, 2009. PSCE'09. IEEE/PES. IEEE, 2009.
- [6] J. C. S. Silva, A. De Conti, D. G. Silveira and J. L. Silvino, "Power transformer modeling based on wide band impedance and admittance measurements," 2013 International Symposium on Lightning Protection (XII SIPDA), Belo Horizonte, 2013, pp. 291-296.
- [7] P. T. M. Vaessen, "Transformer model for high frequencies," in IEEE Transactions on Power Delivery, vol. 3, no. 4, pp. 1761-1768, Oct 1988. doi: 10.1109/61.193982
- [8] Borghetti, A. et al. "Calculation of voltages induced by nearby lightning on overhead lines terminated on distribution transformers". Proceedings of the International Conference on Power Systems Transients. pp. 311-316, Lisbon, 1995
- [9] A. Piantini, C. V. S. Malagodi, "Modeling of Three-Phase Distribution Transformers for Calculating Lightning Induced Voltages Transferred to the Secondary", IEEE, 5th International Symposium on Lightning Protection, Sao Paulo, 1999.
- [10] A. Piantini and C. V. S. Malagodi, "Voltage surges transferred to the secondary of distribution transformers," 1999 Eleventh International Symposium on High Voltage Engineering, London, 1999, pp. 365-368 vol. 1. doi: 10.1049/cp: 19990582
- [11] N. Abed and O. Mohammed, "Physics-based high-frequency transformer modeling by finite elements," Magnetics, IEEE Transactionson, vol. 46, no. 8, pp. 3249–3252, 2010.
- [12] N. Abeywickrama, Y. Serdyuk, and S. Gubanski, "High-frequency modeling of power transformers for use in frequency response analysis (fra)," Power Delivery, IEEE Transactions on, vol. 23, no. 4, pp. 2042 – 2049, 2008.
- [13] Sood, Yog Raj, Rajkumar Jarial, and Kapil Gandhi. "Condition monitoring of power transformer using sweep frequency response analysis." MIT International Journal of Electrical and Instrumentation Engineering 1.2 (2011): 80-86.
- [14] A. Holdyk, B. Gustavsen, I. Arana and J. Holboell, "Wideband Modeling of Power Transformers Using Commercial sFRA Equipment," in IEEE Transactions on Power Delivery, vol. 29, no. 3, pp. 1446-1453, June 2014. doi: 10.1109/TPWRD.2014.2303174.
- [15] B. Gustavsen, "Wide band modeling of power transformers," PowerDelivery, IEEE Transactions on, vol. 19, no. 1, pp. 414 – 422, 2004.
- [16] Z. Zhongyuan, L. Fangcheng, and L. Guishu, "A high-frequency circuit model of a potential transformer for the very fast transient simulation in gis," Power Delivery, IEEE Transactions on, vol. 23, no. 4, pp. 1995 – 1999, 2008.
- [17] Heindl, M., S. Tenbohlen, and R. Wimmer. "Transformer modeling based on standard frequency response measurements." International Symposium on High Voltage Engineering, Hannover, Germany. 2011.
- [18] R. Aghmasheh; V. Rashtchi; E. Rahimpour, "Gray Box Modeling of Power Transformer Windings for Transient Studies," in IEEE Transactions on Power Delivery, vol. PP, no.99, pp.1-1 doi: 10.1109/TPWRD.2017.2649484
- [19] Jurišić, Bruno. "Transformer model for calculation of high frequency, transmitted overvoltages."
- [20] T. Noda, H. Nakamoto and S. Yokoyama, "Accurate modeling of core-type distribution transformers for electromagnetic transient studies," in IEEE Transactions on Power Delivery, vol. 17, no. 4, pp. 969-976, Oct 2002.
- [21] T. Župan, B. Trkulja, R. Obrist, T. Franz, B. Cranganu-Cretu, and J. Smajic, "Transformer Windings Parameters Calculation and Lightning Impulse Voltage Distribution Simulation," IEEE Transactions on Magnetics, vol. 52, no. 3, pp. 1–4, Mar. 2016.
- [22] Bigdeli, Mehdi, and Ebrahim Rahimpour. "Optimized Modeling of Transformer in Transient State with Genetic Algorithm." International Journal of Energy Engineering 2.3 (2012): 108-113.
- [23] J. Chong and A. Abu-Sia da, "A Novel Algorithm to detect Internal Transformer Faults", IEEE Trans. Power Delivery, 2011
- [24] Filipović-Grčić, Dalibor, Božidar Filipović-Grčić, and Ivo Uglešić. "High-frequency model of the power transformer based on frequency-response measurements." IEEE Transactions on Power Delivery 30.1 (2015): 34-42.
- [25] Y. J. Yin, J. P. Zhan, C. X. GU, Q. H. Wu and J. M. Zhang "Multi-Kernel Support Vector Classifier for Fault Diagnosis of Transformers", IEEE Trans. Power Delivery, 2012, vol.21, no.5; May 2013.
- [26] Paulraj. T, Hari Kishan Surjith. P and Dhana Sekaran. P, "Modeling and location of faults in power transformer using Transfer Function and Frequency Response Analysis," 2014 IEEE International Conference on Advanced Communications, Control and Computing Technologies, Ramanathapuram, 2014, pp. 83-87.



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