



# Novel Application of Whale-Optimization-Algorithm Integrated with Local Search Deterministic Techniques to Solve Economic-Load-Dispatch-Problem with Valve-Point-Loading-Effect and Gaseous Emission

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**Abstract**— Amidst the prevailing energy crisis have thus pulled the thermal power plants to come into strike in order to overcome the aforementioned issue seriously have invited ecological problem in parallel and is swelling day by day. Economic load dispatch (ELD) and economic emission dispatch (EED) are the Bi-objective opposite natured functions to each other which are brought into a single function with the aid of scaling factor (SF) and price penalty factor (PPF) to overcome the contradictory natures of fuel cost and emission levels at the same instant while keeping the alternators in their rated constraints of inequality in terms of maximum and minimum power levels and power balance constraint as well as including/excluding the phenomena of valve point loading effects (VPLE). Thus both the functions are balanced at specific single point which not only cuts down the fossil fuel cost but also keeps in parallel the emission level of gaseous products at minimum. Hybridized optimization technique is proposed in this research that carries the capability to combine the nature inspired Whale optimization algorithm with the three specific local search techniques i-e interior point algorithm (IPA), sequential quadratic programming (SQP) and active set (AS) and have been applied on two test cases for cost effective solution.

**Keywords**— Thermal Power Plant, Economic Load Dispatch, Economic Emission Dispatch, Whale Optimization Algorithm, Local Search Techniques, Valve Point Loading Effect.

## I. INTRODUCTION

Economic load dispatch is one of the major functions of electrical power management systems. In electric power industry efficient, high quality, reliable supply and optimum operation of electrical power generation is demanded by utilities so for this purpose the power production level of multiple coupled alternators in an interrelated power

production system are scheduled in such a manner that the operating cost of the system is reduced and entire power demand is fulfilled subjected to satisfaction of all affiliated distinct constraints of power balance and generation capacity linked to electrical power generation units and plant are contented is called as problem of economic load dispatch [1]. The purpose of economic load dispatch is to find out the operating policy for “NG” number of generators that which generator will produce how much power. The following diagram clearly visualizes the scenario.

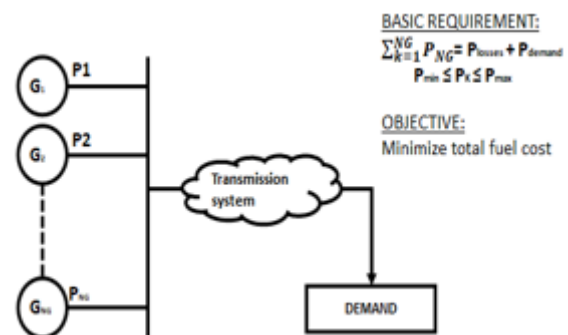


Figure 1: Policy of Economic Load Dispatch

With a rapid increase in population and commercialization, the electrical power demand raises day by day while fossil fuels are already high-priced so there should be an unavoidable need to cut down the operational cost of production in respect of fossil fuel cost. Fossil fuel are burnt in the furnace of thermal power plants emitting several toxic gases like carbon dioxide (CO<sub>2</sub>), silicon dioxide (SO<sub>2</sub>) and nitrogen dioxide (NO<sub>2</sub>) in the chimney promoting another serious issue called “global warming” when released into atmosphere. Due to the increased thermal power plants penetration, the level of gaseous emissions has been exponentially increased within no time [2]. So In order to challenge the reduction of the operational cost concurrently with the level of gaseous emissions into the air

and afore said ecological effects, economic load dispatch concerned problem is reshaped into a latest expression and is labeled to be the problem of Combined Economic Emission Load Dispatch (CEELD). So this problem considering emissions not only reduces the level of gaseous emissions, but also have the ability to curtail the fuel cost magnificently.

Due to the involved natural complexities in traditional optimization techniques, a Hybridized optimization technique is developed that is capable to combine whale optimization algorithm with local search methods for cost effective solution.

## II. SYSTEM MODE

### A. Economic load dispatch Problem

The main objective of economic load dispatch problem is to schedule the generators power output at lower possible fuel cost. Characteristic equation of fuel cost as quadratic polynomial along with the valve point loading effect as sine term can be formulated as follows,

$$\text{Min } C_v(P) = \sum_K^{NG} C_K P_K = \sum_{k=1}^{NG} (a_k P_k^2 + b_k P_k + c_k + |d_k \times \sin(e_k \times (P_k^{\min} - P_k))|) \quad (1)$$

Where  $a_k$ ,  $b_k$  and  $c_k$  are the related fuel cost coefficients of  $k$ th generator in \$/MW<sup>2</sup>h, \$/MW/h and \$/h respectively while  $d_k$  and  $e_k$  are the related coefficients of valve point loading effect in \$/h and rad. “ $P_k$ ” is the variable power output assigned to each ganarator in MW,  $P_{kmin}$  and  $P_{kmax}$  denoting maximum and minimum power output limits while  $C(P)$  on the left hand side of the above equation gives the specified total fuel cost of power system in \$/h for “NG” generators [3].

### B. Economic Emission Dispatch problem

Similarly economic emission dispatch is the function to curtail the level of gaseous emissions as minimum possible while satisfying the demanded load. EED problem can be expressed mathematically as follows,

$$\text{Min } E_v(P) = \sum_{k=1}^{NG} E_k(P_k) = \sum_{k=1}^{NG} (a_{ek} P_k^2 + b_{ek} P_k + c_{ek} + d_{ek} \times \exp(f_{ek} \times P_k)) \quad (2)$$

$a_{ek}$ ,  $b_{ek}$ ,  $c_{ek}$ ,  $d_{ek}$  and  $f_{ek}$  are the coefficients of gaseous emissions expressed in ton/MW<sup>2</sup>h, ton/MWh, ton/h respectively while  $E_v(P)$  on the left hand side is expressed as the total level of emission in tons/h.

### C. Combined Economic Emission Load Dispatch problem

In need to reduce the fossil fuel cost and degree of gaseous discharge simultaneously while keeping in mind

both the equality and inequality constraints, both the objective functions of ELD and EED are combined together by introduction of price penalty factor (PPF), whereas for their contradictory nature, scaling factor (SF) is inserted, the so called as problem of (CEELD), which is a real-world many-objective optimization problem shown below

$$\text{Min } (F_{C.E.E.L.D}) = W * C_v(P) + (1 - W)(P.P.F)_k * E_v(P) \quad (3)$$

Where

$$(P.P.F)_k = \frac{C_v(P_k^{\max})}{E_v(P_k^{\max})} \quad (4)$$

## III. HYBRIDIZED WOA TECHIQUE

Whales are considered to be the largest and longest amongst all the mammals and thus has been categorized into seven distinct species of blue, Minke, killer, finback, humpback, sei and right. These fancy gigantic mammals are assumed to be an intelligent and smart like a human being due to the presence of spindle cells in their brain twice in count than a human adult. They are responsible to develop their emotions, judgment and social behavior like a human being. Whales can live in a family or live alone depending upon the specie. Adult humpback whale is found to be a school bus Equivalent in length and are being grazed on krill and small fish herds present on the surface of water. The unique mechanism of Bubble\_net\_Feeding has been detected uniquely in humpback specie in which they start to dive about 12m deep inside the water when prey is sighted. Humpback then travel upward towards the targeted prey following two types of manoeuvres [4].

### A. Shrinking Surrounding Mechanism

This mechanism employs the following equation in which the value of “ $\vec{a}$ ” is dropped down from 2 to 0 in iterations which in turn effects the value of arbitrary “ $\vec{A}$ ” in interval [-a,a] decreased too. Thus mentioning the value of “ $\vec{A}$ ” in [-1,1] any location can be achieved from the location of search agent towards the best agent location. The equations below shows the achievable position of search agent towards the best agent location in 2D between  $0 \leq A \leq 1$ .

$$\vec{D} = |\vec{C} \cdot \vec{X}_{arb} - \vec{X}| \quad (4)$$

$$\vec{X}(t+1) = \vec{X}_{arb} - \vec{A} \cdot \vec{D} \quad (5)$$

Vector  $\vec{A}$  and  $\vec{C}$  can be find out with the help of equations given below.

$$\vec{A} = 2\vec{a} \cdot \vec{r} - \vec{a} \quad (6)$$

$$\vec{C} = 2 \cdot \vec{r} \quad (7)$$

### B. Spiral Updating Mechanism

A coil shaped path between the original position of whale and targeted position of prey is followed in this spiral updating mechanism with the help of a spiral equation subjected below,

$$\vec{X}(t+1) = \vec{F}.e^{cl} . \cos ine(2. \pi. l) + \vec{X}^*(t) \quad (8)$$

“T” in [-1,1] denotes arbitrary number, “c” is a scalar identifying logarithmic spiral shape while  $\vec{F} = |\vec{X}^*(t) - \vec{X}(t)|$  describes gap between the targeted prey and the kth humpback.

Humpback whale while on its journey towards its targeted prey follow together their spiral shaped and shrinking encircling paths assumed to have 50% chances of selection each at the same time while designing their hunting technique mathematically expressed as follows

$$\vec{X}(t+1) = \begin{cases} \vec{X}^*(t) - \vec{A}.\vec{D} & \text{when } q < 0.5 \\ \vec{F}.e^{cl} . \cos(2\pi l) + \vec{X}^*(t) & \text{when } q \geq 0.5 \end{cases} \quad (9)$$

### IV. SIMULATION RESULTS AND DISCUSSION

This section illustrates the detailed results of simulation tested upon 2 cases discussed below.

#### A. Case 1: System of 3 Generators

In this case, 3 generator units for ELD problem subjected with and without valve point loading effect with load demand of 850 MW is examined. For the 2-test case systems i-e 3 and 6 units, their corresponding generation power limits and scalar coefficients of fuel cost and emission level have been obtained from [5]. Both the cases including and excluding the phenomena of valve point loading effect compiled for 100 independent runs limited to 500 iterations maximum per run where the search agents are kept to 15000 with VPLe phenomena whereas 7500 for without VPLe phenomena.

TABLE 1: INEQUALITY CONSTRAINTS, FUEL COST AND VPLe COEFFICIENTS FOR SYSTEM OF 3-GENERATORS TEST

G.N	Generator Bound limits	a x10 <sup>-3</sup>	b	c x10 <sup>2</sup>	d	e x10 <sup>-3</sup>
G1	100-600	1.56	7.92	5.61	300	31.5
G2	100-400	1.94	7.85	3.10	200	42
G3	50-200	4.82	7.97	0.78	150	63

TABLE 2: COMBINED REFINED RESULTS OF TEST CASE 1 WITHOUT VPLe

Power (MW)	WOA			WOA Hybridized with		
	Best	Mean	worst	IPA	SQP	AS
P1	391.	400.	600.	393.	393.	393.
	7667	0000	0000	1698	1698	1698
P2	344.	400.	100.	334.	334.	334.
	1687	0000	0000	6038	6038	6038
P3	114.	50.	150.	122.	122.	122.
	0646	0000	0000	2264	2264	2264
Total power	850.	850.	850.	850.	850.	850.
	0000	0000	0000	0000	0000	0000
Cost \$/h	8194.	8227.	8371.	8194.	8194.	8194.
	8578	8700	6700	3561	3561	3561
T (sec)	0.7046	0.7400	0.7011	0.100 5	0.0593	0.0357

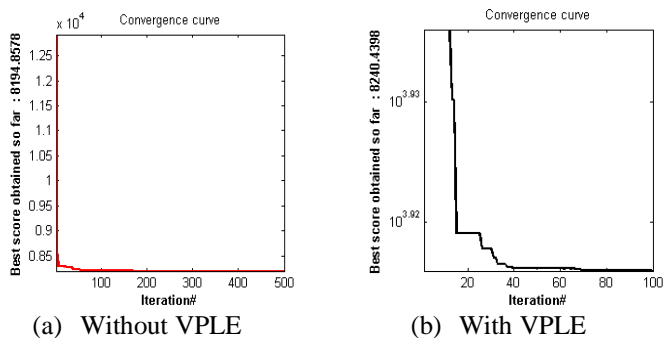


Figure 2: Learning curve for test case 1

Simulation results for whale optimization algorithm alone interms of best, mean and worst, and in hybridized form with three local search techniques are tabulated in table 2&3 along with levels of power assigned to each and every generator and execution time for the load demand of 850MW with and without considering the phenomena of valve point loading effect. Learning curve for test case 1 is shown in figure 2 whereas results for 100 independent runs for both the cases including/excluding VPLe Phenomena are showing in figure 3&4.

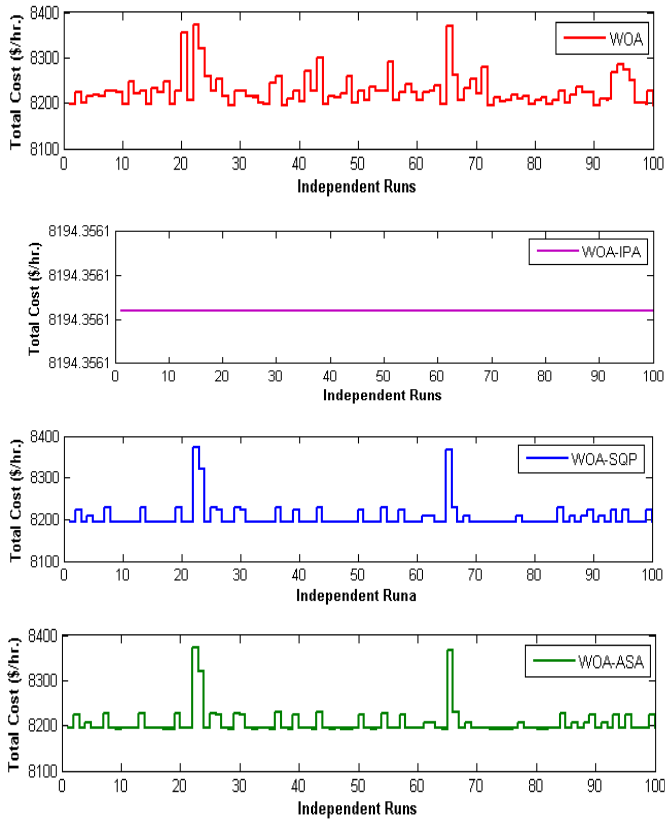


Figure 3: 100 independent runs for test case 1 without VPLE.

TABLE 3: COMBINED REFINED RESULTS OF TEST CASE 1 WITH VPLE.

Power (MW)	WOA			WOA Hybridized with		
	Best	Medium	worst	IPA	SQP	AS
P1	300.	392.	423.	300.	300.	300.
	6138	3836	5195	2668	2668	1957
P2	400.	257.	226.	400.	400.	400.
	0000	6164	4805	0000	0000	0000
P3	149.	200.	200.	149.	149.	149.
	3862	0000	0000	7332	7332	8043
Total Power	850	850	850	850	850	850
cost	8240.	8368.	8624.	8234.	8234.	8234.

\$/h	4398	7836	4998	0718	0718	1115
T(sec)	0.2770	0.2800	0.277 3	0.0838	0.0841	0.0490

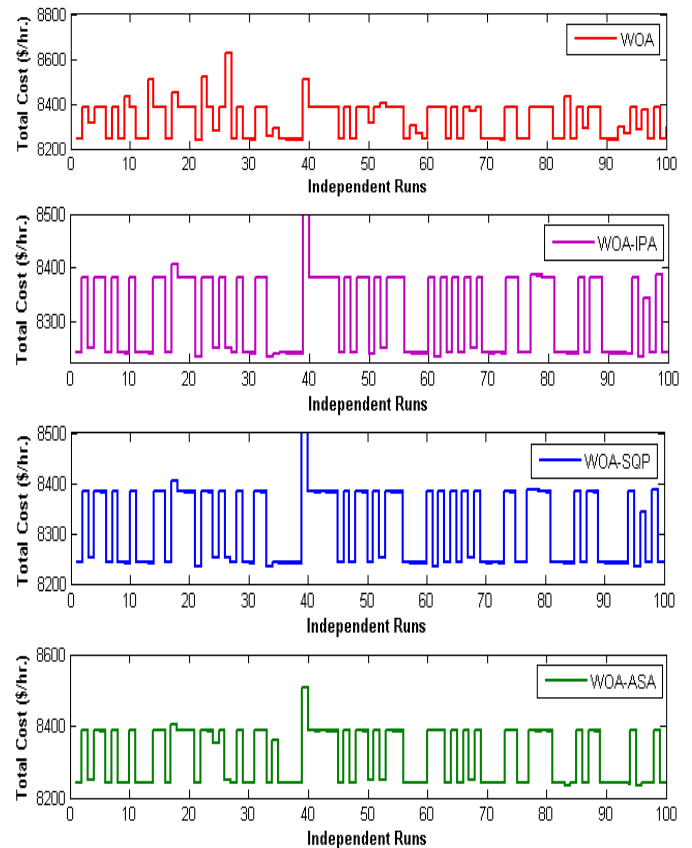


Figure 4: 100 independent runs for test case 1 with VPLE

### B. Case 2: System of 6 Generators

This test case consists of 6 generator units for combined economic emission dispatch (CEELD) problem without valve point loading effect (VPLE) having the required power demand of 1000 MW. The required data has been tabulated below in table 4. At scaling factor SF=1, CEELD problem becomes economic load dispatch (ELD) problem which cuts down fuel cost to 5039.6315 \$/h but increases emission levels to 978.8066 ton/h. Conversely at scaling factor SF=0, it becomes economic emission dispatch (EED) problem decreasing down emission level to 800.1264 ton/h but increases fuel cost to 5211.1423 \$/h.

Learning curve for test case 2 is shown in figure 5 while the Simulation results relating the proposed Algorithm for the cost of fuel and gaseous emissions are mentioned in table 5.

TABLE 4: INEQUALITY CONSTRAINTS, FUEL COST COEFFICIENTS AND EMISSION COEFFICIENTS FOR SYSTEM OF 6-GENERATORS TEST

G.N	Generator Bound limits	a	b	c x10 <sup>3</sup>	ae	Be x10 <sup>-3</sup>	ce x10 <sup>3</sup>
G1	10-125	756.8	38.540	152.5	13.860	330	4.2
G2	10-150	451.325	46.160	106	13.860	330	4.2
G3	35-225	1050.0	40.400	28	40.267	545.5	6.8
G4	35-210	1243.53	38.310	35.5	40.267	545.5	6.8
G5	130-325	1658.57	36.328	21.1	42.900	511.2	4.6
G6	125-315	1356.66	38.270	18	42.900	511.2	4.6

TABLE 5: COMBINED REFINED RESULTS OF TEST CASE 2 WITHOUT VPLe

S.F	Megawatts allocated to each and every generator for P <sub>D</sub> =1000MW						Cost \$/h	EmissionTons/h
	G1	G2	G3	G4	G5	G6		
0	100.	104.	166.	166.	228.	232.	5211.	800.
	7180	5094	7849	9590	8116	2171	1423	1264
.1	82.	95.	160.	146.	253.	260.	5150.	819.
	7954	7914	4211	5920	7708	6293	5907	7198
.2	61.	92.	197.	148.	274.	226.	5128.	847.
	4815	3611	1234	0541	0373	9426	4269	7854
.3	57.	120.	157.	165.	242.	255.	5175.	824.
	7113	0979	8813	8447	9844	4804	4062	2638
.4	94.	73.	165.	159.	272.	235.	5138.	827.
	3480	5812	1936	1398	5470	1904	9258	0479
.5	79.	73.	152.	164.	255.	275.	5111.	839.
	5469	4171	2838	0147	3650	3725	7421	3119
.6	61.	59.	151.	172.	274.	279.	5073.	870.
	5374	9085	9599	4086	8620	3236	9744	4544
.7	55.	88.	178.	151.	280.	244.	5110.	849.
	9275	6383	7685	6686	5957	4014	9701	9554
.8	76.	59.	160.	177.	228.	297.	5099.	861.
	5679	3863	3021	2455	8013	6969	6485	9298
.9	61.	31.	162.	169.	284.	290.	5052.	905.
	0173	5855	5899	4998	7081	5994	2486	6545
1	30.	23.	173.	142.	319.	309.	5039.	978.
	7412	4987	4407	8450	6550	8194	6315	8066

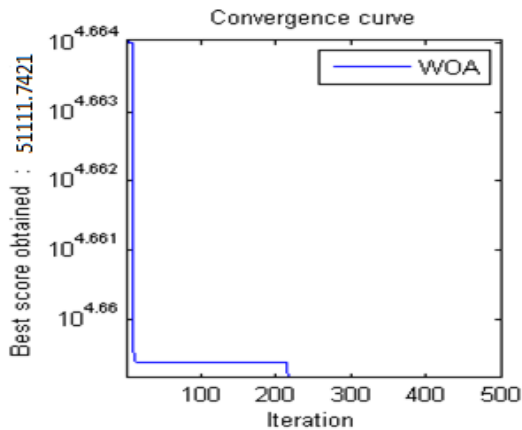


Figure 5: Learning curve for test case 2

### CONCUSLION

This paper analyzes two test case systems for economic load dispatch and combined economic emission load dispatch problems having distinct power load demands. Test case 1 contains the proposed algorithm alone and in hybridized form both for the cases with and without VPLE Phenomena. Without considering the Valve point loading effect, above table 2 shows best, mean and worst fuel cost results for whale optimization algorithm and hybridized whale optimization algorithm showing that the best score achieved for W.O.A alone is 8194.8578 \$/h. "S.Q.P", "A.S" and "I.P.A" are known as local search techniques which have the capability to reduce down the cost more when hybridized with Whale algorithm of optimization. All the three local search techniques integrated with W.O.A tabulated the same fuel cost results of 8194.3561\$/h and thus showed their optimality. On the other hand, Taking into account the phenomena of valve point loading effect, the simulation results are listed above in table 3 The best score achieved for W.O.A is 8240.4398 \$/h executed in 0.2770 seconds Whale optimization algorithm admits 8234.0718 \$/h hybridized with local search techniques I.P.A & S.Q.P while A.S hybridization admitted 8234.1115 \$/h. Thus it is clear from the table that W.O.A-I.P.A & S.Q.P proved to be more cost effective and optimum compared to W.O.A by tailoring the fuel cost from 8240.4398 \$/h to 8234.0718 \$/h. Similarly in test case 2, at scaling factor 1 and 0, the established function converts wholly to ELD and EED problems respectively due to their contradictory natures thus to overcome the unbalanced phenomena between fuel cost and emission level

SF=0.5 is selected that makes the functions mutually stable to cut down the fuel cost and emissions volume at the same time.

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